



**Itasdi**

Innovative Teaching Approaches in development of Software  
Designed Instrumentation and its application in real-time  
systems

# Theory of Robotics Systems

Kinematic control of  
differential drive mobile robot

Co-funded by the  
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## Innovative Teaching Approaches in development of Software Designed Instrumentation and its application in real-time systems

Faculty of Technical  
Sciences



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University  
Faculty of Electrical Engineering  
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Zagreb University of  
Applied Sciences



School of Electrical  
Engineering  
University of Belgrade



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# Teorija Robotskih Sistema

Kinematska kontrola

mobilnih robota sa diferencijalnim pogonom

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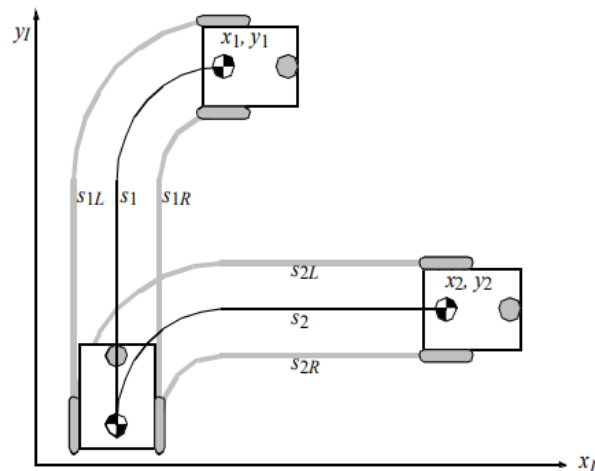


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# Kinematika mobilnih robota

- Kinematika manipulatora vs kinematika mobilnih robota
  - Predstavljaju odnos između unutrašnjih i spoljašnjih koordianta
  - Kod mobilnih robota, očitavanja sa enkodera ne mapiraju kretanje u jedinstvenu poziciju u prostoru – Ne postoji direktan način merenja pozicije robota već se pozicija dobija integraljenjem i zavisi pređenog puta.





# Forward Kinematics – Inverse Kinematics

- Forward Kinematics:
  - Vrší transformacii iz unutrašnjih koordinata u spoljašnje:  
brzina točkova → brzina robota
- Inverse Kinematics:
  - Transformacija iz spoljašnjih koordinata u unutrašnje (potrebna je za implementaciju kontrolera):  
brzina robota → brzina točkova



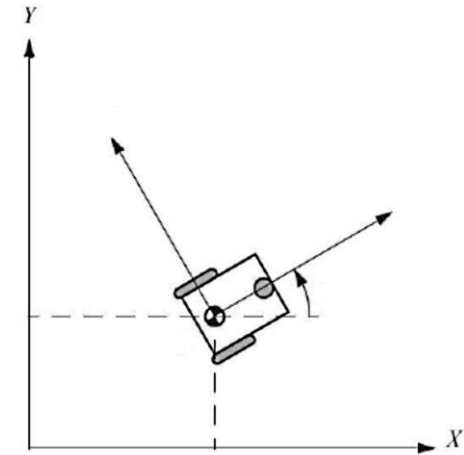


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# Kinematika mobilnog robota sa diferencijalnim pogonom

- Imamo kontrolu nad ugaonim brzinama levog i desnog točka, a želimo da kontrolišemo  $x, y$  poziciju robota i njegovu orijentaciju u toj poziciji.
- Odnos brzina točkova određuje na koji će se način robot kretati.



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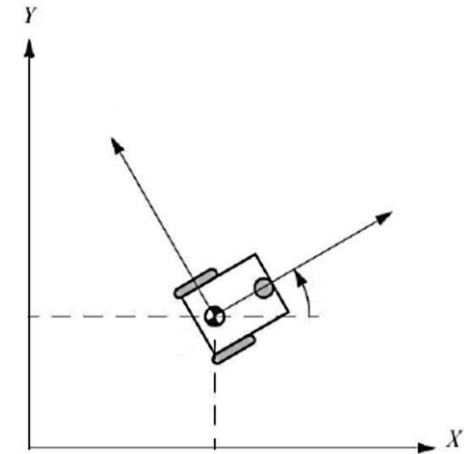


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# Feedforward kontrola

- Upotreba: Udaljena kontrola robota, predefinisani oblik trajektorije.
- $v = \frac{r\dot{\phi}_R + r\dot{\phi}_L}{2}$ ,  $\omega = \frac{r\dot{\phi}_R - r\dot{\phi}_L}{l}$
- Putanja se mora podeliti u jasne segmente: prave linije ili delove kruga.
- Izračunavanje brzina točkova prema zadatoj putanji pre pokretanja programa.
- Nedostaci:
  - Izračunavanje ostvarive trajektorije nekada može da bude težak zadatak.
  - Adaptacija na dinamičke promene u okruženju nije moguća.
  - Rezultujuća trajektorija u krajnjem slučaju nije glatka.



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# Upravljanje u zatvorenoj sprezi

$$\begin{bmatrix} v(t) \\ \omega(t) \end{bmatrix} = K \cdot e = K \cdot \begin{bmatrix} x \\ y \\ \theta \end{bmatrix}^R$$

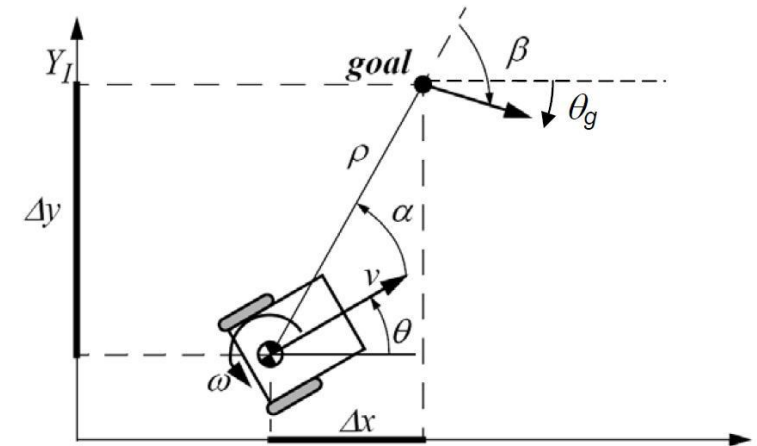
Potrebno je pronaći takvu matricu  $K$ , koja će određenog vremena dovesti grešku na nulu.

$$\rho = \sqrt{\Delta x^2 + \Delta y^2}$$

$$\alpha = -\theta + \text{atan2}(\Delta y, \Delta x)$$

$$\beta = -\theta - \alpha$$

Transformacija u polarne koordinate



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# Upravljanje u zatvorenoj sprezi

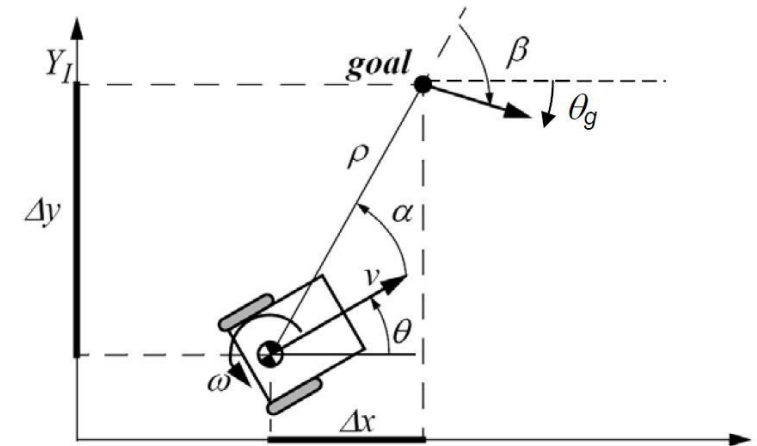
Prelaskom na polarne koordinate translatornu i rotacionu izražavamo:

$$v = k_{\rho}\rho \quad \omega = k_{\alpha}\alpha + k_{\beta}\beta$$

Gde sistem u zatvorenoj sprezi ima oblik:

$$\begin{bmatrix} \dot{\rho} \\ \dot{\alpha} \\ \dot{\beta} \end{bmatrix} = \begin{bmatrix} -k_{\rho}\rho \cos\alpha \\ k_{\rho}\sin\alpha - k_{\alpha}\alpha - k_{\beta}\beta \\ -k_{\rho}\sin\alpha \end{bmatrix}$$

$$k_{\rho} > 0 ; \quad -k_{\beta} > 0 ; \quad k_{\alpha} - k_{\rho} > 0$$



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# TurtleBot3 paketi

- Instalacija svih ROS paketa na koje se oslanjaju TurtleBot3 paketi:
  - Neki od paketa su: kontrola džojstikom, kontrola LIDAR-a, podrška za arduino platformu, paketi za mapiranje i navigaciju, ...
- Instalacija svih potrebnih paketa za rad sa realnim i simuliranim robotom.

[Link](#) sa detaljnim uputstvom.



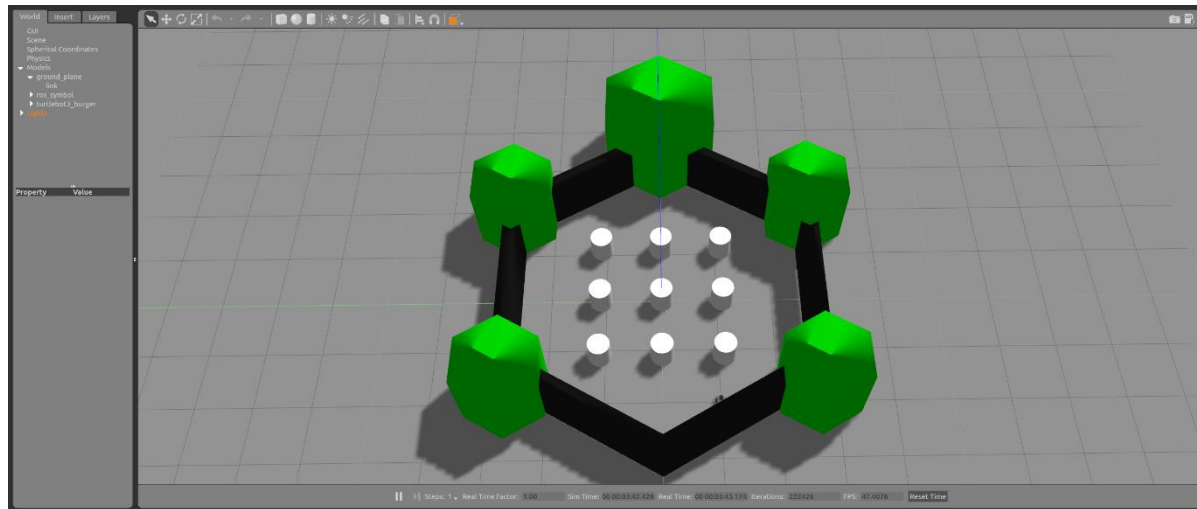


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# TurtleBot3 i Gazebo

- export TURTLEBOT3\_MODEL=Burger
- Roslaunch turtlebot3\_gazebo turtlebot3\_world.launch



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# Povezivanje sa TurtleBot3 robotom

- Više uređaja preko mreže može činiti jednu celinu ROS sistema.
- PC podešavanja:
  - `bashrc : export ROS_HOSTNAME=ip_of_remote_PC`  
`export ROS_MASTER_URI=http:// ip_of_remote_PC:11311`
- TurtleBot3 podešavanja:
  - `bashrc: export ROS_HOSTNAME=ip_of_TURTLEBOT`  
`export ROS_MASTER_URI=http://ip_of_remote_PC:11311`





# Povezivanje sa TurtleBot3 robotom

- Pokrećemo master nod: roscore
- Pristupamo konzoli na robotu: `ssh username@IPadresaRobota`  
`ssh vitezkoja@192.168.0.5 (pass: zamlata)`
  - Iz terminala koji je povezan sa robotom poziva se osnovni nod koji pokreće sve funkcionalnosti robota: `roslaunch turtlebot3_bringup turtlebot3_robot.launch`
- Nakon toga se mogu pozivati nodovi koji će komunicirati sa robotom
  - `roslaunch turtlebot3_teleop turtlebor3_teleop_key.launch`



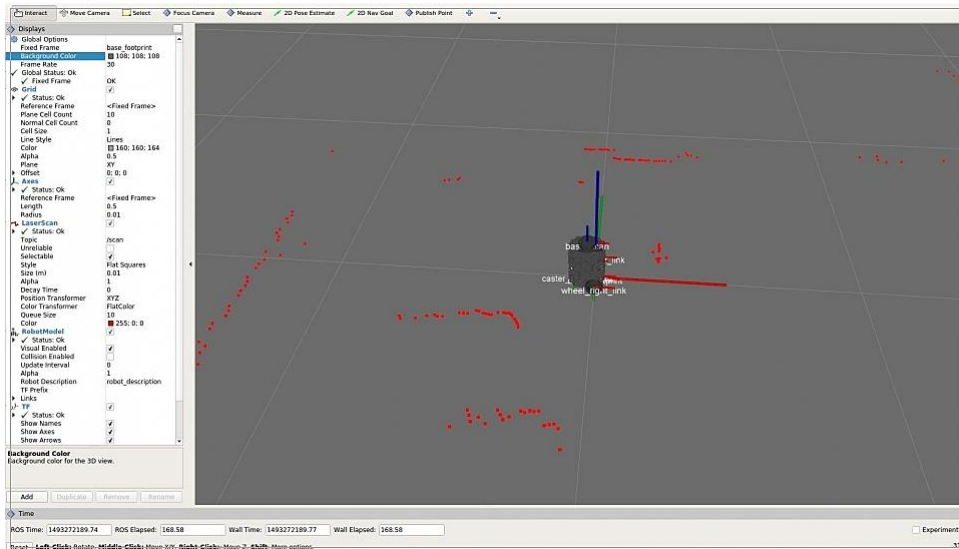


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# Vizuelizacija sa senzora

- export TURTLEBOT3\_MODEL=Burger
- Roslanuch turtlebot3\_bringup turtlebot3\_remote.launch
- Rosrun rviz rviz -d `rospack find turtlebot3\_description`/rviz/model.rviz



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Thanks!

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